Random Testing in 321

## Test Cases So Far

Each test relates a particular input to a particular output.
(test (bound-ids (with 'x (id 'y) (id 'x))) '(x))
(test (binding-ids (with 'x (id 'y) (id 'x)))
'(x))

## Property-based Testing

But we can only write so many tests by hand.

To find additional bugs, we can automate testing.

We start with what we hope is a fact about our program.

For example,
"If bound-ids says ' $x$ is bound, then binding-ids says ' $x$ is binding."

## Property Violation

If we can find some WAE for which the property doesn't hold ...

$$
\begin{aligned}
& \text { (define a-WAE ...) } \\
& \text { (bound-ids a-WAE) ; } \Rightarrow{ }^{\prime}(x) \\
& \text { (binding-ids a-WAE) } \Rightarrow{ }^{\prime}()
\end{aligned}
$$

... we've found a bug.

## Property Testing

We can test this property in the usual style.
; bound=>binding? : WAE -> boolean
; checks if bound ids are also binding (define (bound=>binding? e) ...)
(test (bound=>binding? (id 'x)) true)
(test (bound=>binding?

$$
\begin{aligned}
& \text { (with 'x (num 0) (id 'x))) } \\
& \text { true) }
\end{aligned}
$$

Expected result is always true, so if we had lots of WAEs, then we'd have lots of tests.

## Automated Property Testing

Write a program to generate test inputs!

## Random WAEs

```
; random-WAE: -> WAE
(define (random-WAE)
    (case (random 5)
    [(0) (num (random-nat))]
    [(1) (id (random-symbol))]
    [(2) (add (random-WAE) (random-WAE))]
    [(3) (sub (random-WAE) (random-WAE))]
    [(4) (with (random-symbol)
        (random-WAE)
        (random-WAE))]))
```

Watch out - that code is buggy.... (read on for why)

## Random WAEs

; random-nat: -> nat
(define (random-nat)
(case (random 2)
[ (0) 0]
[(1) (add1 (random-nat))]))
; random-symbol: -> symbol
(define (random-symbol)
(random-elem '( $x$ y z a bc)))
; random-elem: (listof X$) ~->\mathrm{X}$
(define (random-elem xs)
(list-ref xs (random (length xs))))

## Generation Strategy

To build a WAE,

- I/5 of the time, build a number
- I/5 of the time, build a symbol
- 3/5 of the time, first build two more WAEs


## Expected Progress

On average, we "reduce" the problem from

Generate I WAE.

to

## Generate I. 2 WAEs.

since $1.2=(2 / 5) * 0+(3 / 5) * 2$

## Height Bound

Limit WAE size by bounding tree height.

```
; random-WAE/b: nat -> WAE
(define (random-WAE/b h)
    (case (random (if (zero? h) 2 5))
    [(0) (num (random-nat))]
    [(1) (id (random-symbol))]
    [(2) (add (random-WAE/b (sub1 h))
        (random-WAE/b (sub1 h)))]
    [(3) (sub (random-WAE/b (sub1 h))
    (random-WAE/b (sub1 h)))]
    [(4) (with (random-symbol)
    (random-WAE/b (sub1 h))
    (random-WAE/b (sub1 h)))]))
```

(Alternatively, tweak weights.)

## Property Implementation

; bound=>binding: WAE -> boolean
(define (bound=>binding e) (sublist? (bound-ids e) (binding-ids e)))
; sublist?: (listof X) (listof X) -> boolean
; Expects xs and ys to be sorted and have no dups.
(define (sublist? xs ys)
(cond [(null? xs) \#t]
[(null? ys) \#f]
[ (equal? (car xs) (car ys)) (sublist? (cdr xs) (cdr ys))]
[else (sublist? xs (cdr ys))]))

## Running Tests

; test-bound=>binding: nat nat -> (or 'passed WAE)
(define (test-bound=>binding size attempts)
(if (zero? attempts)
'passed
(let ([test-input (random-WAE/b size)])
(if (bound=>binding test-input) (test-bound=>binding
size
(sub1 attempts))
test-input))))
(test-bound=>binding 5 1000)

## HW2 Test Results

We ran random tests on a past year's HW2 submissions.

- Received 99 submissions (includes multiple attempts from the same person)
- Tested 6 properties
- Found a bug in 53 out of those 99 submissions


## Interpreter Properties

- Interpreter does not crash
- Produces same result as another implementation (e.g., DrRacket)
- Type checker accurately predicts result (later)
- Program equivalences hold


## With Enclosing Example

For example, we should be able to replace any subexpression with a new variable.

$$
\{+12\} \Rightarrow\left\{\begin{aligned}
\{\text { with } & \left\{\begin{array}{ll}
x & 2\} \\
\{+1 & x\}
\end{array}\right\}
\end{aligned}\right.
$$

## Another example:

$$
\begin{aligned}
&\{\text { with }\{x\{+526\}\} \\
&\{-x 4\}\}
\end{aligned}
$$

```
{with {z {+ 5 26}}
    {with {x z}
{- x 4}}}
```


## Transformation Strategy

- Generate a random path for a WAE expression tree
- Pick a subexpression based on the path to bind to a new id
- Replace subexpression with a bound occurrence of the id


## Generating Random Paths

- Automatically pick leaf nodes
- Flip a coin to determine whether we move further down the tree
- Because we are "lifting" a subexpression out of its original context, we only pick expressions which will not contain free id's
- Always pick the named-expr of the first with we encounter


## Path Generation Implementation

; coin-flip: boolean
(define (coin-flip)
(zero? (random 2)))
; weighted-chance: number $->$ boolean
(define (weighted-chance pct)
(<= (random) (/ pct 100)))

## Path Generation Implementation

; random-path: WAE -> (listof symbol)
(define (random-path wae)
(type-case WAE wae
[num (n) empty]
[id (x) empty]
[with (name named-expr body) '(left)]
[else
(if (weighted-chance 20)
empty

(cons 'right
(random-path (get-branch 'right wae) ) ) ) (])

## Path Generation Implementation

; get-branch: symbol WAE -> WAE
(define (get-branch choice wae)
(type-case WAE wae
[add (lhs rhs) (case choice
[(left) lhs]
[(right) rhs])]
[sub (lhs rhs) (case choice [(left) lhs]
[(right) rhs])]
[with (name named-expr body) (case choice
[(left) named-expr]
[(right) body])]
[else wae]))

## Extracting the Subexpression

Given a path, we find the subexpression:

```
; pick-subexpr: WAE (listof symbol) -> WAE
(define (pick-subexpr wae path)
    (cond
    [(empty? path) wae]
    [else
        (pick-subexpr (get-branch (car path) wae)
                                (cdr path))]))
```


## Replacing with the New ID

; swap-subexpr WAE (listof symbol) symbol -> WAE
(define (swap-subexpr wae path new-id)
(cond
[ (empty? path) (id new-id)]
[else
(type-case WAE wae
[add (lhs rhs)
(swap-in-bop path new-id add lhs rhs)]
[sub (lhs rhs)
(swap-in-bop path new-id sub lhs rhs)]
[with (name named-expr body) (with name
(id new-id)
body) ]
[else wae])])

## Replacing with the New ID

```
(define (swap-in-bop path new-id op lhs rhs)
    (case (car path)
    [(left) (op (swap-subexpr lhs
                                (cdr path)
                                new-id)
    rhs)]
    [(right) (op lhs
    (swap-subexpr rhs
        (cdr path)
        new-id))])
```


## Implementing the Transformation

```
; rand-sym-not-in: (listof symbol) -> symbol
(define (rand-sym-not-in lst)
    (let ([leftover (remove* lst syms)])
        (list-ref leftover
    (random (length leftover)))))
; wae->with-wae: WAE -> WAE
(define (wae->with-wae wae)
    (let* ([path (random-path wae)]
            [subexpr (pick-subexpr wae path)]
            [new-id (rand-sym-not-in (binding-ids wae))])
    (with new-id
    subexpr
    (swap-subexpr wae path new-id))))
```


## Putting It All Together

We generate 1000 WAE's and compare interpreter output for the original and transformed programs:

```
(for ([i (in-range 0 1000)])
    (let* ([wae (random-WAE/b 2 '())]
    [new-wae (wae->with-wae wae)])
    (test (interp wae)
    (interp new-wae))))
```


## What Went Wrong?

- Our random WAE generator builds arbitrary expressions
- Probability we generate a WAE with free identifiers is very high

Eliminating Free ID's from the Random Generator
; rand-sym-from: (listof symbol) -> symbol
(define (rand-sym-from ss)
(list-ref ss (random (length ss))))

## Eliminating Free ID's from the Random Generator

```
(define (random-WAE/b h bindingids)
    (case (random (if (zero? h) 2 5))
    [(0) (num (random-nat))]
    [(1) (if (empty? bindingids)
    (num (random-nat))
    (id (rand-sym-from bindingids)))]
    [(2) (add (random-WAE/b (sub1 h) bindingids)
        (random-WAE/b (sub1 h) bindingids))]
    [(3) (sub (random-WAE/b (sub1 h) bindingids)
        (random-WAE/b (sub1 h) bindingids))]
    [(4) (let ([new-id (random-symbol)])
        (with new-id
            (random-WAE/b (sub1 h) bindingids)
            (random-WAE/b (sub1 h)
                                (cons new-id
                                bindingids))) )] ) )
```

